

**LESSON**  
**3-3**

**Interpreting the Unit Rate as Slope**

**Reteach**

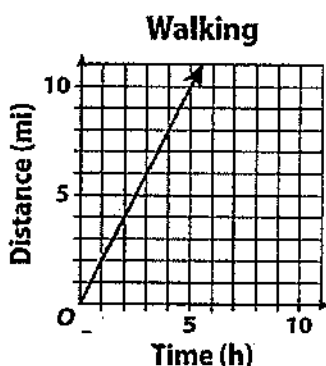
A rate is a comparison of two quantities that have different units.

A **unit rate** is a rate in which the second quantity is 1 unit.

For example, walking 10 miles every 5 hours is a rate. Walking 2 miles every 1 hour is the equivalent unit rate.

$$\frac{10 \text{ miles}}{5 \text{ hours}} = \frac{2 \text{ miles}}{1 \text{ hour}} = 2 \text{ mi/h}$$

The slope of a graph represents the unit rate. To find the unit rate, find the slope.



Step 1: Use the origin and another point to find the slope.

$$\text{slope} = \frac{\text{rise}}{\text{run}} = \frac{10 - 0}{5 - 0} = \frac{10}{5} = 2$$

Step 2: Write the slope as the unit rate.

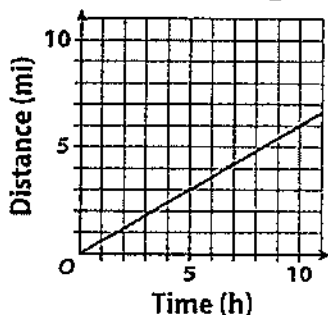
$$\text{slope} = \text{unit rate} = 2 \text{ mi/h}$$

*★ Any questions please  
Contact Mr. Watson  
on the Remind App.*

*Students,  
I hope  
each and  
every one  
of you are  
doing good  
and staying  
safe. I'm*

Find the slope of the graph and the unit rate.

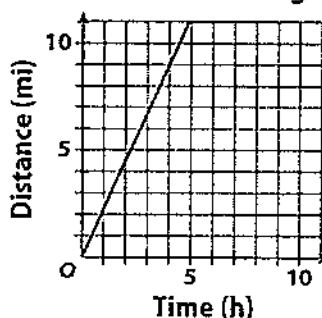
1. **Scott Hiking**



slope =  $\frac{\text{rise}}{\text{run}} =$  \_\_\_\_\_

unit rate = \_\_\_\_\_ mi/h

2. **Rebecca Hiking**



slope =  $\frac{\text{rise}}{\text{run}} =$  \_\_\_\_\_

unit rate = \_\_\_\_\_ mi/h

*very proud of  
all of you for  
the hardwork  
you have given  
me. Know we  
are always thinking  
of you. I am  
always here if  
you need anything*

*Best Wishes,  
Mr. Watson*

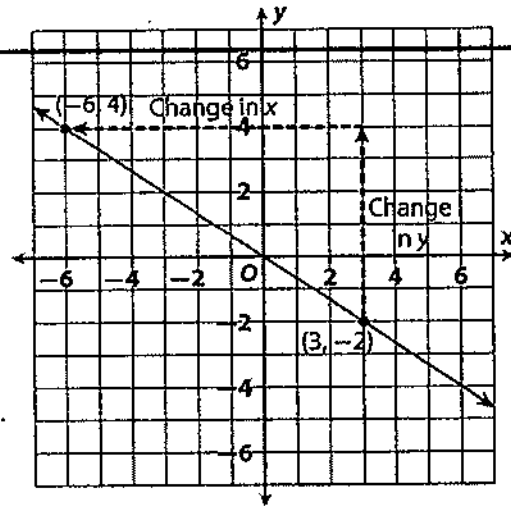
**LESSON** **Rate of Change and Slope**

**3-2**

*Reteach*

Look at the relationships between the table, the graph, and the slope.

First value ( $x$ )	Second value ( $y$ )
-6	4
-3	2
0	0
3	-2



To find the slope, choose two points, using the table or graph. For example, choose  $(-6, 4)$  and  $(3, -2)$ .

Change in  $y$ :  $4 - (-2) = 6$

Change in  $x$ :  $-6 - 3 = -9$

$$\text{Slope} = \frac{\text{change in } y}{\text{change in } x} = \frac{6}{-9} = -\frac{2}{3}$$

Use the example above to complete Exercises 1 and 2.

- The slope is negative. In the table, as the values of  $x$  decrease, the values of  $y$  \_\_\_\_\_.
- The slope is negative. In the graph, as you move from left to right, the line of the graph is going \_\_\_\_\_ (up or down).

Solve.

- Suppose the slope of a line is positive. Describe what happens to the value of  $x$  as the value of  $y$  increases.

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- Suppose the slope of a line is positive. Describe what happens to the graph of the line as you move from left to right.

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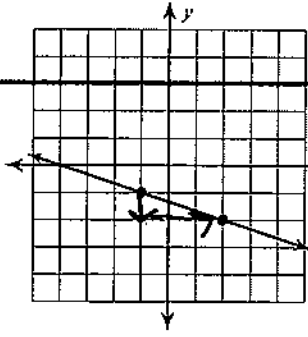
- Two points on a line are  $(3, 8)$  and  $(-3, 2)$ . What is the slope of the line?

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# Slope

Find the slope of each line. \* use  $\frac{\text{rise}}{\text{run}}$

1)

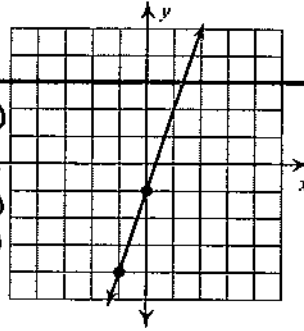


\* reminder work  
left → right

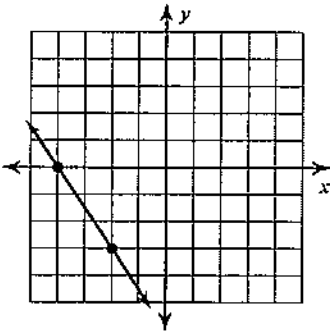
down 1  
right 3  
down (negative)  
up (positive)  
left (negative)  
right (positive)

$-\frac{1}{3}$  \* remember to  
reduce if possible

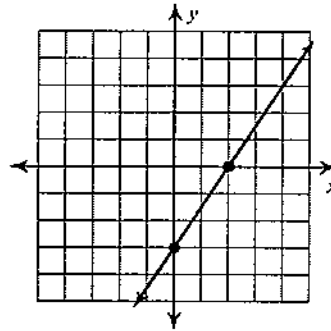
2)



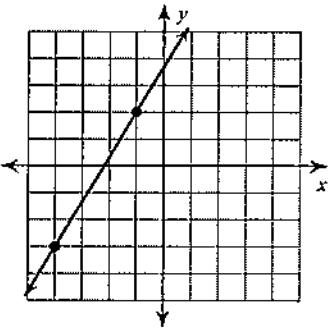
3)



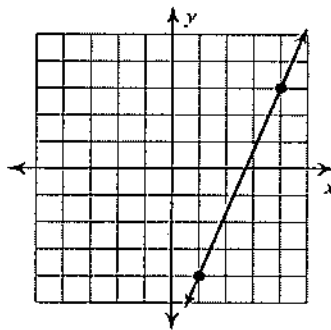
4)



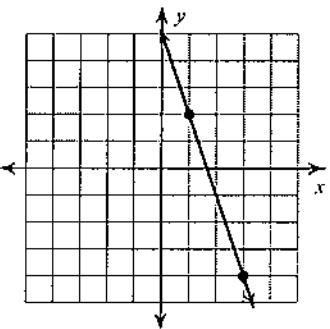
5)



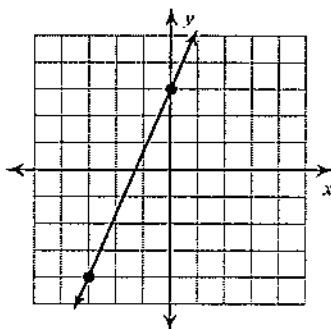
6)



7)



8)



**LESSON**  
**4-1**

**Representing Linear Nonproportional Relationships**

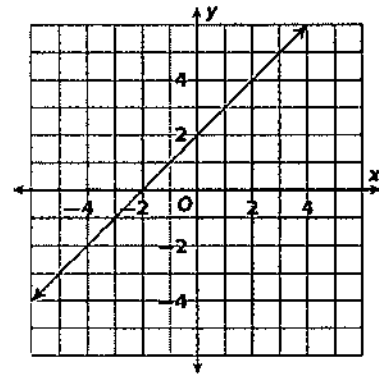
*Reteach*

A relationship will be proportional if the ratios in a table of values of the relationship are constant. The graph of a proportional relationship will be a straight line through the origin. If either of these is not true, the relationship is nonproportional.

To graph the solutions of an equation, make a table of values. Choose values that will give integer solutions.

A. Graph the solutions of  $y = x + 2$ .

$x$	-2	-1	0	1	2
$y$	0	1	2	3	4



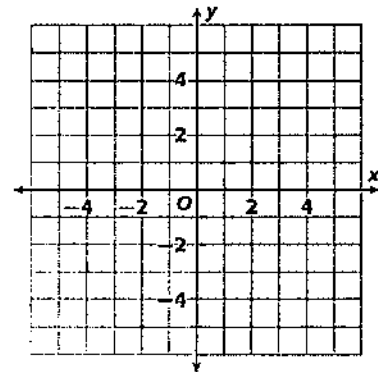
B. Tell whether the relationship is proportional. Explain.

The graph is a straight line, but it does not go through the origin, so the relationship is not proportional.

Make a table and graph the solutions of each equation.

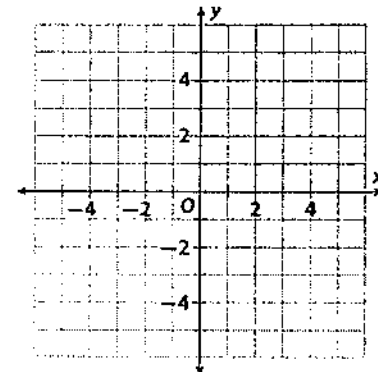
1.  $y = 3x + 1$

$x$	-2	-1	0	1	2
$y$					



2.  $y = -x - 2$

$x$	-2	-1	0	1	2
$y$					



Find the slope of the line through each pair of points.

$$\frac{Y_2 - Y_1}{X_2 - X_1}$$

20

9)  $(8, 10), (-7, 14)$

\* reduce if possible

10)  $(-3, 1), (-17, 2)$

$$\frac{Y_2 - Y_1}{X_2 - X_1} \text{ Plug In } \rightarrow \frac{14 - 10}{-7 - 8} = \frac{4}{-15}$$

11)  $(-20, -4), (-12, -10)$

12)  $(-12, -5), (0, -8)$

13)  $(-19, -6), (15, 16)$

14)  $(-6, 9), (7, -9)$

15)  $(-18, -20), (-18, -15)$

16)  $(12, -18), (11, 12)$

Find the slope of each line.  $y = mx + b$

$m = \text{slope}$   $y = y\text{-int}$

17)  $y = -5x - 1$

Slope =

y-int =

18)  $y = \frac{1}{3}x - 4$

Slope =

y-int =

19)  $y = -\frac{1}{5}x - 4$

Slope =

y-int =

20)  $y = 1$

Slope =

y-int =

21)  $y = \frac{1}{4}x + 1$

Slope =

y-int =

22)  $y = -\frac{2}{3}x - 1$

Slope =

y-int =

23)  $y = -x + 2$

Slope =

y-int =

24)  $y = -x - 1$

Slope =

y-int =

25)  $2x + 3y = 9$  \* write in  $y = mx + b$

26)  $5x + 2y = 6$  \* write in  $y = mx + b$

**LESSON**  
**5-2**

# Writing Linear Equations from a Table

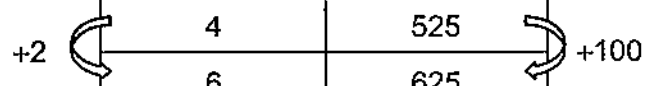
## Reteach

A linear relationship can be described using an equation in slope-intercept form,  $y = mx + b$ , where  $m$  is the slope and  $b$  is the  $y$ -intercept. Recall that the  $y$ -intercept  $b$  is where the graph of the equation crosses the  $y$ -axis, which is at point  $(0, b)$ .

The table below shows the linear relationship between the hours it takes to repair a car and the total cost of the repairs, including the cost of the parts.

Look for an  $x$ -value of 0. The corresponding  $y$ -value, 325, is the  $y$ -intercept.

Hours Worked, $x$	Total Cost (\$), $y$
0	325
2	425
4	525
6	625



Find changes in  $x$ -values and  $y$ -values. Then use the values to find the slope:

$$m = \frac{\text{change in } y\text{-values}}{\text{change in } x\text{-values}} = \frac{100}{2} = 50$$

Using  $x$ -values that differ by 1 will require the least calculation.

Use the  $y$ -intercept,  $b = 325$ , and the slope,  $m = 50$  to write an equation for the relationship.

$$y = mx + b$$

$$y = 50x + 325$$

Write an equation in slope-intercept form for each linear relationship.

- The total monthly cost,  $y$ , for smartphone service depends on the number of text messages,  $x$ .

slope: \_\_\_\_\_

Text Messages, $x$	0	10	20	30
Cost (\$), $y$	40.00	42.00	44.00	46.00

$y$ -intercept: \_\_\_\_\_

equation: \_\_\_\_\_

- The total cost,  $y$ , for a taxi ride depends on the number of miles traveled,  $x$ .

slope: \_\_\_\_\_

Distance (mi), $x$	0	1	5	10
Total Cost (\$), $y$	2.50	5.00	15.00	27.50

$y$ -intercept: \_\_\_\_\_

equation: \_\_\_\_\_



**LESSON**  
**4-3**

# Graphing Linear Nonproportional Relationships Using Slope and y-Intercept

## Reteach

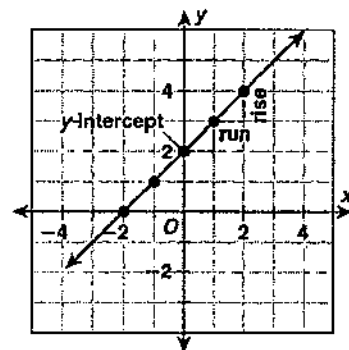
You can graph a linear function by graphing the y-intercept of the line and then using the slope to find other points on the line.

The graph shows  $y = x + 2$ .

To graph the line, first graph the y-intercept which is located at  $(0, 2)$ .

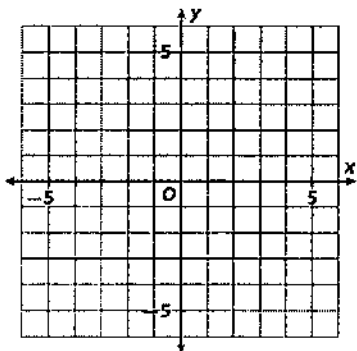
Because the slope is 1 or  $\frac{1}{1}$ , from the y-intercept, rise 1 and run 1 to graph the next point.

Connect the points with a straight line.



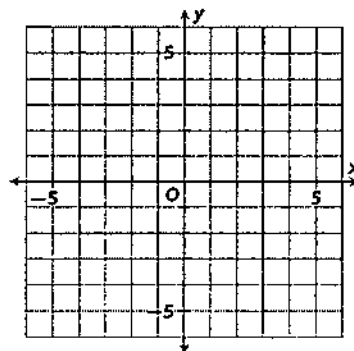
Graph each equation using the slope and the y-intercept.

1.  $y = 4x - 1$



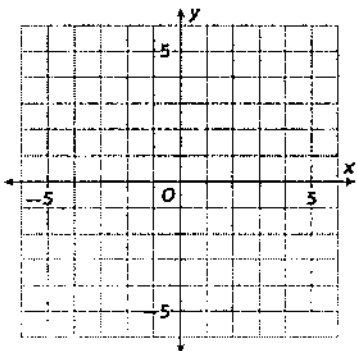
slope = \_\_\_\_\_ y-intercept = \_\_\_\_\_

2.  $y = -\frac{1}{2}x + 2$



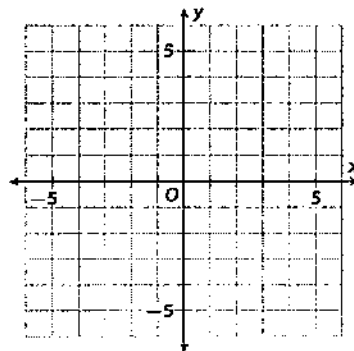
slope = \_\_\_\_\_ y-intercept = \_\_\_\_\_

3.  $y = -x + 1$



slope = \_\_\_\_\_ y-intercept = \_\_\_\_\_

4.  $y = 2x - 3$



slope = \_\_\_\_\_ y-intercept = \_\_\_\_\_

## Proportions

State if each pair of ratios forms a proportion.

1)  $\frac{4}{2}$  and  $\frac{20}{6}$

$$\begin{array}{r} 4 \times 6 \\ \hline 24 \end{array} \quad ? \quad \begin{array}{r} 2 \times 20 \\ \hline 40 \end{array}$$

★ cross-multiply.

★ if they equal each other they are proportional.

★ Is the answer to number 1 proportional?

3)  $\frac{4}{3}$  and  $\frac{16}{12}$

4)  $\frac{4}{3}$  and  $\frac{8}{6}$

5)  $\frac{12}{24}$  and  $\frac{3}{4}$

6)  $\frac{6}{9}$  and  $\frac{2}{3}$

Solve each proportion. (cross multiply and divide)

7)  $\frac{10}{k} = \frac{8}{4}$

$10 \times 4 \div 8$

?

8)  $\frac{m}{10} = \frac{10}{5}$

9) .

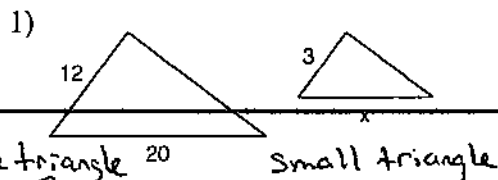
$\frac{v}{12} = \frac{10}{2}$

10)  $\frac{3}{x} = \frac{6}{10}$



# Similar Figures

Each pair of figures is similar. Find the missing side.



★ set up a proportion  
★ pick sides that match up.

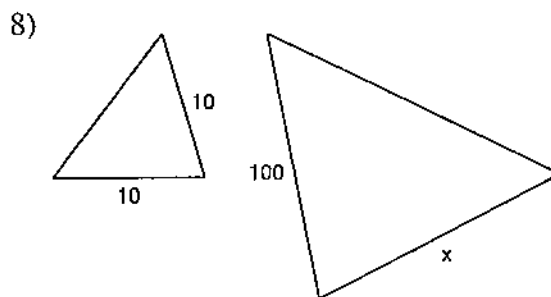
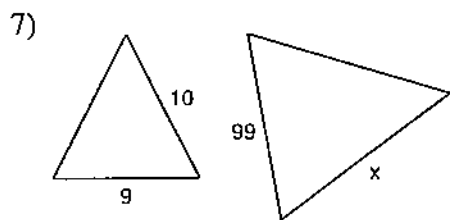
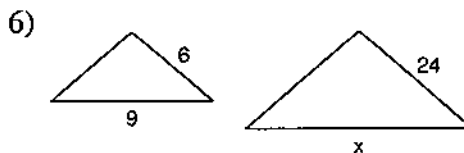
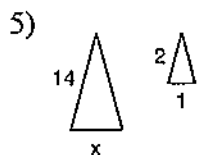
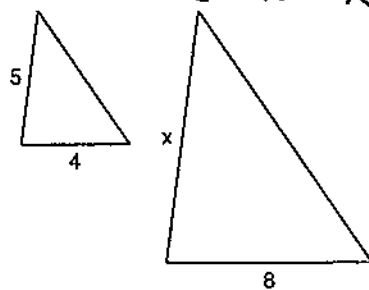
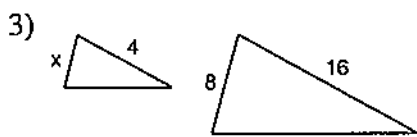
\* 12 on the big triangle matches 3 on the small one so we put those at the top.

\* 20 on the big triangle matches X on the small one. Now put those on the bottom.

★ final step cross multiply and divide to solve for X.

$$\frac{12}{20} = \frac{3}{x}$$

$$20 \times 3 \div 12 = \underline{\hspace{2cm}}$$





**LESSON**  
**11-3**

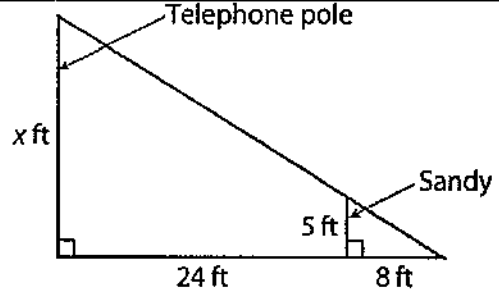
# Angle-Angle Similarity

## Reteach

When solving triangle similarity problems involving proportions, you can use a table to organize given information and set up a proportion.

A telephone pole casts the shadow shown on the diagram. At the same time of day, Sandy, who is 5 feet tall, casts a shadow 8 feet long, as shown. Find the height of the telephone pole.

**Organize distances in a table.**  
Then use the table to write a proportion.



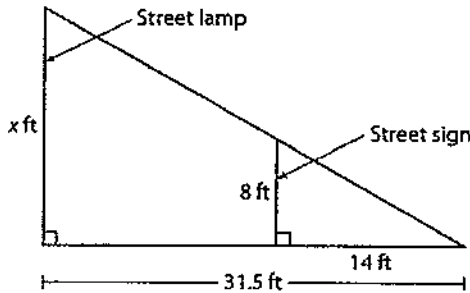
	Pole	Sandy
Height (ft)	x	5
Length of shadow (ft)	24 + 8, or 32	8

$$\frac{x}{32} = \frac{5}{8}$$

Solve the proportion. The height of the telephone pole is 20 feet.

Complete the table. Then find the unknown distance.

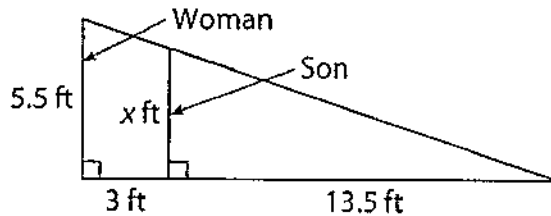
1. A street lamp casts a shadow 31.5 feet long, while an 8-foot tall street sign casts a shadow 14 feet long.



	Lamp	Sign
Height (ft)		
Length of shadow (ft)		

Height of street lamp = \_\_\_\_\_

2. A 5.5-foot woman casts a shadow that is 3 feet longer than her son's shadow. The son casts a shadow 13.5 feet long.



	Woman	Son
Height (ft)		
Length of shadow (ft)		

Height of son = \_\_\_\_\_

**LESSON** **11-2** **Angle Theorems for Triangles**

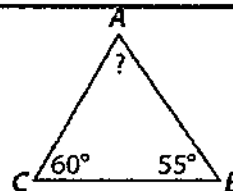
**Reteach**

If you know the measure of two angles in a triangle, you can subtract their sum from  $180^\circ$ . The difference is the measure of the third angle.

The two known angles are  $60^\circ$  and  $55^\circ$ .

$$60^\circ + 55^\circ = 115^\circ$$

$$180^\circ - 115^\circ = 65^\circ$$



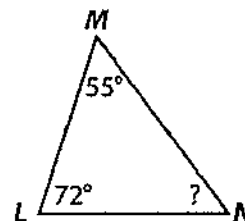
**Solve.**

1. Find the measure of the unknown angle.

Add the two known angles:  $\underline{\quad} + \underline{\quad} = \underline{\quad}$

Subtract the sum from  $180^\circ$ :  $180 - \underline{\quad} = \underline{\quad}$

The measure of the unknown angle is:  $\underline{\quad}$

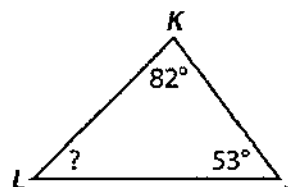


2. Find the measure of the unknown angle.

Add the two known angles:  $\underline{\quad} + \underline{\quad} = \underline{\quad}$

Subtract the sum from  $180^\circ$ :  $180 - \underline{\quad} = \underline{\quad}$

The measure of the unknown angle is:  $\underline{\quad}$



$\angle DEG$  is an exterior angle.

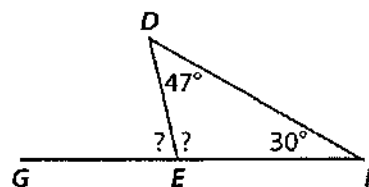
The measure of  $\angle DEG$  is equal to the sum of  $\angle D$  and  $\angle F$ .

$$47^\circ + 30^\circ = 77^\circ$$

You can find the measure of  $\angle DEF$  by subtracting  $77^\circ$  from  $180^\circ$ .

$$180^\circ - 77^\circ = 103^\circ$$

The measure of  $\angle DEF$  is  $103^\circ$ .



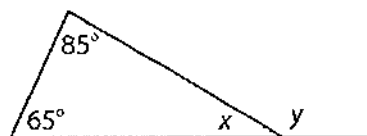
**Solve.**

3. Find the measure of angle  $y$ .

$$85^\circ + 65^\circ = \underline{\hspace{2cm}}$$

4. Find the measure of angle  $x$ .

$$180^\circ - \underline{\quad} = \underline{\quad}$$



Name \_\_\_\_\_

(27)

## Order of Operations

Date \_\_\_\_\_ Period \_\_\_\_\_

Evaluate each expression.

use PEMDAS. Show all work,

1)  $(30 - 3) \div 3$

2)  $(21 - 5) \div 8$

3)  $1 + 7^2$

4)  $5 \times 4 - 8$

5)  $8 + 6 \times 9$

6)  $3 + 17 \times 5$

7)  $7 + 12 \times 11$

8)  $15 + 40 \div 20$

9)  $20 + 16 - 15$

10)  $19 - 15 - 3$

11)  $9 \times (3 + 3) \div 6$

12)  $(9 + 18 - 3) \div 8$

## Evaluating Variable Expressions

Evaluate each using the values given.

1)  $n^2 - m$ ; use  $m = 7$ , and  $n = 8$

$$8^2 - 7$$

$$8 \cdot 8 = 64$$

$$64 - 7$$

$$57$$

- ★ replace the letter with the number
- ★ Then use order of operations to solve
- ★ Show all work.

3)  $yx \div 2$ ; use  $x = 7$ , and  $y = 2$

4)  $m - n \div 4$ ; use  $m = 5$ , and  $n = 8$

5)  $x - y + 6$ ; use  $x = 6$ , and  $y = 1$

6)  $z + x^3$ ; use  $x = 1$ , and  $z = 19$

7)  $y + yx$ ; use  $x = 15$ , and  $y = 8$

8)  $q \div 6 + p$ ; use  $p = 10$ , and  $q = 12$

9)  $x + 8 - y$ ; use  $x = 20$ , and  $y = 17$

10)  $15 - (m + p)$ ; use  $m = 3$ , and  $p = 10$

11)  $10 - x + y \div 2$ ; use  $x = 5$ , and  $y = 2$

12)  $p - 2 + qp$ ; use  $p = 7$ , and  $q = 4$

## The Distributive Property (Show all work)

Simplify each expression.

$$1) \begin{array}{l} \textcircled{6} \textcircled{1} \textcircled{5m} \\ \downarrow \quad \downarrow \\ 6(1) - 6(5m) \end{array}$$

$$6 - 30m$$

\* Pass out the 6 using multiplication. Remember to pass out to all numbers in the ( ).  
 \* remember combining like terms. We can NOT put 6 and  $-30m$  together with addition or subtraction

3)  $3(4 + 3r)$

4)  $3(6r + 8)$

5)  $4(8n + 2)$

6)  $-(-2 - n)$

7)  $-6(7k + 11)$

8)  $-3(7n + 1)$

9)  $-6(1 + 11b)$

10)  $-10(a - 5)$

11)  $-3(1 + 2v)$

12)  $-4(3x + 2)$

13)  $(3 - 7k) \cdot -2$

14)  $-20(8x + 20)$

15)  $(7 + 19b) \cdot -15$

16)  $(x + 1) \cdot 14$

## Two-Step Equations With Integers (Show all work) Date \_\_\_\_\_ Period \_\_\_\_\_

Solve each equation.

$$1) \frac{r}{10} + 4 = 5$$


---


$$\frac{r}{10} - 4 = 5 - 4$$


---


$$\frac{r}{10} = 1$$


---


$$r = 10$$

- ① Draw a line
- ② subtract 4 off both sides
- ③ leaves  $\frac{r}{10} = 1$
- ④ multiply both sides by 10
- ⑤ leaves  $r = 10$

3)  $3p - 2 = -29$

4)  $1 - r = -5$

5)  $\frac{k-10}{2} = -7$

6)  $\frac{n-5}{2} = 5$

7)  $-9 + \frac{n}{4} = -7$

8)  $\frac{9+m}{3} = 2$

9)  $\frac{-5+x}{22} = -1$

10)  $4n - 9 = -9$

11)  $\frac{x+9}{2} = 3$

12)  $\frac{-12+x}{11} = -3$

13)  $\frac{-4+x}{2} = 6$

14)  $-5 + \frac{n}{3} = 0$

